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# Low Temperature Heat Capacity of Layered Superconductors SrNi<sub>2</sub>Ge<sub>2</sub> and SrPd<sub>2</sub>Ge<sub>2</sub>

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Abstract Low-temperature heat capacity C(T) of the weakly electron-correlated SrNi<sub>2</sub>Ge<sub>2</sub> 122-layer compound undergoes a superconducting transition with onset at 1.4 K and a bulk  $T_c = 0.75$  K, where heat-capacity jump ratio  $\Delta C(T_c)/\gamma T_c = 0.88$ –1.05. A small average superconducting energy gap  $E_g(\text{ave}) = 2.21 \ kT_c = 0.14 \text{ meV}$  is derived for this multi-gap superconductor. Similar results for isostructural SrPd<sub>2</sub>Ge<sub>2</sub> include  $T_c(\text{onset}) = 3.5$  K, bulk  $T_c$  of 2.92 K,  $\Delta C(T_c)/\gamma T_c = 0.70$  and  $E_g(\text{ave}) = 2.54 \ kT_c = 0.64 \text{ meV}$ . The higher  $T_c$  onset could be associated with stoichiometric 1:2:2 grains in the polycrystalline samples. In addition, deviations of  $E_g/kT_c$  from the BCS ratio of 3.5 suggest that, just like their iron-based counterpart, these 122-layer germanides may also exhibit an unconventional, fully-opened multi-gap *s*-wave superconductivity.

Keywords Superconducting materials · Heat capacity · 122-layer germanide

## 1 Introduction

The discovery of high temperature superconductivity with transition temperatures  $T_c$  up to 55 K in strongly electron-correlated LaFeAs( $O_{1-x}F_x$ ) has generated a profound interest in iron-based layer systems [1].

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For the Co-doped  $A(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$  (A = Ca, Sr, Ba) 122-layer system with the ThCr<sub>2</sub>Si<sub>2</sub>-type body-centered-tetragonal (bct) structure (space group I4/mmm),  $T_c$  up to 22 K was observed near the antiferromagnetic spin density wave (SDW) transition of the undoped  $A\text{Fe}_2\text{As}_2$  [2–10]. Local density approximation (LDA) band calculations indicate that the 3*d* electron density of states (DOS) has a downward shift on Co-3*d*<sup>7</sup> bands with a stronger Co-3*d*<sup>7</sup>-As-4*p* hybridization. The LDA Fermi surface shows low dispersive 2D-like *d* bands and Co affects heavy hole-like bands at zone center, but not lighter electron-like bands around zone boundary [2–4].

For the Fe-deficient  $K_{1-x}Fe_{2-y}Se_2$  122-layer system, superconductivity up to 32 K occurs only in the vacancy-free stoichiometric KFe<sub>2</sub>Se<sub>2</sub>, and not in the vacancy-stabilized tetragonal superstructure  $K_{0.8}Fe_{1.6}Se_2$  [11–13].

The disconnected 2D hole- and electron-pockets containing Fermi surface is believed to be the cause of an unconventional multi-gap *s*-wave superconductivity with possible sign-reversal between hole and electron pockets ( $s_{\pm}$ -wave) [14, 15].

Relevant to this study is the occurrence of superconductivity in the germanide system of  $SrT_2Ge_2$  (T = 3d or 4d transition metals) with a similar bct structure where (TGe)<sup>-</sup> layers are separated by  $Sr^{2+}$  layers [16–20].  $T_c$  has been reported to be 3.04 K for  $SrPd_2Ge_2$  [16], and 1.1 K for  $SrNi_2Ge_2$  [18]. Considering the close resemblance in structural symmetry and mechanism of superconductivity between these iron-free compounds and the iron-based 122-layer systems, we have carried out a comprehensive calorimetric study on the superconducting- and normal-state thermal properties of  $SrNi_2Ge_2$  and  $SrPd_2Ge_2$  to supplement earlier preliminary heat capacity measurements.

## 2 Experiment

Ternary  $SrT_2Ge_2$  samples (T = Ni or Pd) were prepared by two-step arc melting under argon atmosphere. High purity Ni or Pd (>99.9 %) was first arc melted with Ge (99.9999 %) to form an intermediate compound TGe, which was then melted together with Sr (99.5 %). Extra Sr was added to compensate for the evaporation loss due to high vapor pressure at melting, thus ensuring the stoichiometric ratio of Sr:T:Ge = 1:2:2 to within 1 %. X-ray powder-diffraction data were collected by a Rigaku Rotaflex 18-kW rotating anode diffractometer.

Low-temperature heat capacity measurements down to 0.3 K and in applied fields up to 1 T were made in a <sup>3</sup>He cryostat using a thermal relaxation method with a RuO<sub>2</sub> thin-film thermometer. Additional characterizations include electrical resistance measurements down to 0.4 K by the standard four-probe method, and low-field magnetic susceptibility measurements down to 2 K by using a Quantum Design 1-T  $\mu$ -metal shielded MPMS<sub>2</sub> Superconducting Quantum Interference Device (SQUID) magnetometer.

## **3** Results and Discussion

The as-melted polycrystalline samples show single-phase bct structure (space group I4/mmm) with tetragonal lattice parameters a = 0.4160(4) nm, c = 1.0187(10) nm



Fig. 2 Electrical resistance of SrNi<sub>2</sub>Ge<sub>2</sub> indicates a  $T_c$  onset of 1.1 K. The molar magnetic susceptibility of SrPd2Ge2 indicates a T<sub>c</sub> onset of 3.2 K at 10 G (Color figure online)

for  $SrNi_2Ge_2$  and a = 0.4397(4) nm, c = 1.0065(10) nm for  $SrPd_2Ge_2$ . Their lowtemperature heat capacity C(T) data are shown in Fig. 1. A bulk-superconducting heat-capacity jump  $\Delta C = 12.0$  mJ/mol K prevails in SrNi<sub>2</sub>Ge<sub>2</sub> at the midpoint  $T_c =$ 0.75 K of a transition width of 0.72-0.78 K. This new specimen presents the same onset  $T_c = 0.78$  K as the previous measurement [20]. For SrPd<sub>2</sub>Ge<sub>2</sub>, similar results yield  $\Delta C = 37.1$  mJ/mol K,  $T_c = 2.92$  K and a transition width of 2.85–2.96 K.

Corroborative evidence of the of the superconducting transition is given in Fig. 2. The electrical resistance of  $SrNi_2Ge_2$  indicates a  $T_c$  onset of 1.1 K with zeroresistance  $T_c(\text{zero}) = 0.87$  K. Due to the short-circuit nature of resistivity measurements, it is not surprising to have the higher  $T_c$  onset, which suggests that as-melted samples with nominal composition  $Sr_{1-x}T_{2-y}Ge_2$  may contain some vacancy-free 1:2:2 stoichiometric phase [13].

For SrPd<sub>2</sub>Ge<sub>2</sub>, a higher T<sub>c</sub> onset of 3.2 K was observed in 10-G low-field magnetic susceptibility measurements as shown in Fig. 2. Large zero-field-cooled (ZFC) shielding signals of  $-7.68 \text{ cm}^3/\text{mol}$  at 2 K and  $-1.26 \text{ cm}^3/\text{mol}$  at 3 K were observed

online)



with field-cooled (FC) Meissner signals of  $-3.53 \text{ cm}^3/\text{mol}$  at 2 K and  $-1.26 \text{ cm}^3/\text{mol}$  at 3 K. The  $T_c$  of 3.2 K is the highest  $T_c$  reported so far for SrPd<sub>2</sub>Ge<sub>2</sub>. Again, this higher  $T_c$  may be associated with some stoichiometric 1:2:2 grains in the polycrystalline samples. No  $T_c$  above 2 K was observed in SrPd<sub>2</sub>Ge<sub>2</sub> at a 1-T applied field.

A C/T versus  $T^2$  plot for SrNi<sub>2</sub>Ge<sub>2</sub> with  $T_c = 0.75$  K is shown in Fig. 3. Above  $T_c$ , the normal-state heat capacity from 1.4 K to 3.2 K can be fitted with the formula  $C_N(T) = C_{eN} + C_{Debye} = \gamma T + \beta T^3$ , with an electronic term coefficient  $\gamma = 15.3$  mJ/mol K<sup>2</sup> and a Debye temperature  $\theta_D = 287$  K from  $\beta = 0.413$ mJ/mol K<sup>4</sup>. A slightly upturn deviation from linearity starts around 1.4 K, which is even higher than the resistivity  $T_c$  onset of 1.1 K. Again, the higher  $T_c$  may be due to some 1:2:2 stoichiometric phase in the polycrystalline sample. The derived superconducting heat-capacity jump ratio  $\Delta C(T_c)/\gamma T_c$  of 1.05 is lower than the BCS value of 1.43.

A  $(C - \beta T^3)/\gamma T_c$  versus  $T/T_c$  plot for SrNi<sub>2</sub>Ge<sub>2</sub> is shown in Fig. 4. Below  $T_c = 0.75$  K, the superconducting electronic heat capacity contribution  $C_{eS}(T) = C_{eS} - \beta T^3$  can be roughly fitted with a simple exponential formula  $C_{eS}/\gamma T_c =$ 



7.01 exp $(-1.10T_c/T)$  which suggests an average superconducting energy gap  $E_g(\text{ave}) = 2.21 \ kT_c = 0.14 \text{ meV}$  for this multi-gap *s*-wave-like superconductor. The ratio  $E_g(\text{ave})/kT_c$  is lower than the BCS value of  $E_g(0)/kT_c = 3.5$ .

A band-structure calculation for  $SrT_2Ge_2$  (T = Ni, Pd) suggests that, with 30 valence electrons per formula unit, as compared to 28 valence electrons for the quasi-2D-like BaFe<sub>2</sub>As<sub>2</sub>, the Fermi level shifts up into the upper manifold of T-nd/Ge-4p hybridized bands where, in addition to  $d_{xy}$  and  $d_{x^2-y^2}$  bands, large contributions exist from  $d_{xz}$ ,  $d_{yz}$ , and  $d_{z^2}$  bands. As a result, the Fermi surface is transformed into a multi-sheet 3D-like structure [17].

The deviations of  $\Delta C(T_c)/\gamma T_c$  and  $E_g/kT_c$  from the BCS values suggest that SrNi<sub>2</sub>Ge2 is of an unconventional multi-gap *s*-wave nature and similar to that of ironbased superconductors [14, 15]. The lower superconducting transition temperature of this electron-overdoped material in the weakly electron-correlated Fermi liquid regime is the direct result of more dispersive 3D-like Fermi surface. The observed  $\gamma$  value of 15.3 mJ/mol K<sup>2</sup> is higher than 7.85 mJ/mol K<sup>2</sup> calculated from the free electron model and indicates the effect of electron-correlation for this multi-gap superconductor.

To check the validity of the fit and the field-dependent superconducting- and normal-state properties,  $C(B_a)/T$  versus  $T^2$  of another SrNi<sub>2</sub>Ge<sub>2</sub> (Sample II) in applied fields  $B_a = 0$ , 80 G, and 1 T are shown in Fig. 5. Identical midpoint  $T_c$  of 0.75 K (inset) with transition width 0.73–0.80 K was observed at zero field, and  $T_c$  decreases to 0.62 K with transition width 0.53–0.71 K in 80 G. Heat-capacity jump onset at 0.57 K was clearly observed in 1-T field with an extrapolated upper critical field  $H_{c2}(0 \text{ K}) = 5 \text{ T}.$ 

The normal-state heat capacity  $C_N(B_a)$  above 1.4 K in three different fields can all be fitted with  $C_N(T) = C_{eN} + C_{Debye} = \gamma T + \beta T^3$  with a slightly larger but field-independent  $\gamma = 17.1$  mJ/mol K<sup>2</sup> and a Debye temperature  $\theta_D = 274$  K from  $\beta = 0.475$  mJ/mol K<sup>4</sup>. Again, an upturn deviation from linearity indicates a  $T_c$  onset around 1.4 K. The superconducting heat-capacity jump ratio  $\Delta C(T_c)/\gamma T_c$  is 0.88. Since both samples show an 122 single phase, the slightly different values observed



may be due to a slight composition variation of  $Sr_{1-x}Ni_{2-y}Ge_2$  in the arc melting processes.

A C/T versus  $T^2$  plot for SrPd<sub>2</sub>Ge<sub>2</sub> having the higher  $T_c = 2.92$  K is shown in Fig. 6. Above  $T_c$ , the normal-state heat capacity from 3.5 K to 6.3 K can also be fitted with the formula  $C_N(T) = \gamma T + \beta T^3$ , but with a larger normal-state electronic coefficient  $\gamma = 18.1$  mJ/mol K<sup>2</sup> and a lower Debye temperature  $\theta_D = 160$  K from  $\beta = 2.38$  mJ/mol K<sup>4</sup>. The upturn deviation from linearity indicates a  $T_c$  onset around 3.5 K which is higher than 3.2 K from the magnetic susceptibility data. This supports our speculation that stoichiometric ratio of 1:2:2 is crucial for an elevated  $T_c$ .

The superconducting specific-heat jump ratio  $\Delta C(T_c)/\gamma T_c$  of 0.70 is even lower than 0.88–1.05 observed for SrNi<sub>2</sub>Ge<sub>2</sub>, further indicating an unconventional nature of *s*-wave superconductivity in these compounds.

A  $(C - \beta T^3)/\gamma T_c$  versus  $T/T_c$  plot for SrPd<sub>2</sub>Ge<sub>2</sub> is shown in Fig. 7. At low temperatures, a Schottky-type contribution is observed and the superconducting-state heat capacity, after having the lattice term substracted,  $C_S - \beta T^3 = C_{eS} + C_{Schottky}$ . However, the Schottky-type contribution decreases rapidly with increasing temperature and becomes totally negligible for T > 1.5 K. As a result, the superconducting electronic heat capacity  $C_{eS}$  above 1.5 K can be roughly fitted with exponential formula  $C_{eS}/\gamma T_c = 7.34 \exp(-1.27T_c/T)$  which corresponds to a larger average superconducting energy gap  $E_e$  (ave) = 2.54  $kT_c = 0.64$  meV.

The additional contribution to the observed heat capacity below 1.5 K increases with decreasing temperature, resembling roughly to the high-temperature tail of a nuclear Schottky term. Without any magnetic ordering of electronic moments to induce a magnetic hyperfine field here, the anomaly is presumably a nuclear quadrupole term, which is caused by the alignment of nuclear quadrupole moment in the electric field gradient of the crystal. Its magnitude relies on the non-zero quadrupole moment and a large electric field gradient at nucleus. Palladium is the most likely source, since it has an isotope, <sup>105</sup>Pd, with higher natural abundance (22.3 %) as well as a larger nuclear quadrupole moment (+6.6 × 10<sup>-29</sup> m<sup>2</sup>) than nickel (<sup>61</sup>Ni, 1.14 %, +1.62 × 10<sup>-29</sup> m<sup>2</sup>), strontium (<sup>87</sup>Sr, 7.0 %, +3.35 × 10<sup>-29</sup> m<sup>2</sup>) or germanium (<sup>73</sup>Ge, 7.73 %, -1.73 × 10<sup>-29</sup> m<sup>2</sup>). Indeed, no similar anomaly was observed in SrNi<sub>2</sub>Ge<sub>2</sub>. The highly anisotropic layered structure of SrPd<sub>2</sub>Ge<sub>2</sub> must be responsible for the large electric field gradient.

The observed  $\gamma$  value of 18.1 mJ/mol K<sup>2</sup> is higher than that of SrNi<sub>2</sub>Ge<sub>2</sub> and much higher than 6.84 mJ/mol K<sup>2</sup> calculated from the free electron model. Previously reported single crystal heat-capacity data with a lower  $T_c$  of 2.67 K in a narrow temperature measurement range from 2 to 3.5 K may be unreliable [19]. Low  $T_c$  suggests that the flux-grown single crystal may not of the stoichiometric 1:2:2 composition. The curve-fitting below heat capacity upturn of 3.5 K had led to an incorrect  $\Delta C(T_c)/\gamma T_c$  value of 2.1 instead of 0.70 revealed in this report.

#### 4 Conclusion

Low-temperature heat capacity C(T) of multi-gap SrNi<sub>2</sub>Ge<sub>2</sub> with  $T_c = 0.75$  K shows a heat-capacity jump ratio  $\Delta C(T_c)/\gamma T_c = 0.88$ –1.05 and an average superconducting energy gap  $E_g(\text{ave}) = 2.21 kT_c = 0.14 \text{ meV}$ . For SrPd<sub>2</sub>Ge<sub>2</sub> with  $T_c = 2.92$  K, the jump ratio is  $\Delta C(T_c)/\gamma T_c = 0.70$  and  $E_g(\text{ave}) = 2.54 kT_c = 0.64$  meV. An observed higher  $T_c$  onset is likely associated with some stoichiometric 1:2:2 grains in the sample. The deviation of  $E_g/kT_c$  from the BCS ratio of 3.5 suggests that these 122-layer germanide compounds may exhibit *s*-wave multi-band superconducting gaps and be of an unconventional *s*-wave nature as proposed for iron-based superconductors.

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